

# Towards silvicultural prescriptions for mixed-species stands

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# Formulas for mixing regulation with the Density equivalence coefficient, DEC

Species proportion of numbers of trees ( $m_{N1}$ ,  $m_{N2}$ , where  $m_{N1}+m_{N2}=1$ )

$$N_{1,(2)} = N_{1,\underline{2}} \times (1/\text{DEC}_{sp_2 \to sp_1} + 1/m_{N_1} - 1)^{-1}$$

$$N_{(1),2} = N_{1,\underline{2}} \times (1/(DEC_{sp_2 \to sp_1} \times m_{N_2}) - 1/DEC_{sp_2 \to sp_1} + 1)^{-1}$$
  

$$N_{1,2} = N_{1,\underline{2}} \times (1/(DEC_{sp_2 \to sp_1} + 1/m_{N_1} - 1)^{-1} + (1/(DEC_{sp_2 \to sp_1} \times m_{N_2}) - 1/DEC_{sp_2 \to sp_1} + 1)^{-1})$$

Species proportion by area ( $m_{A1}$ ,  $m_{A2}$ , where  $m_{A1}+m_{A2}=1$ )

$$N_{1,(2)} = N_{1,\underline{2}} \times m_{A_1} \times DEC_{sp_2 \rightarrow sp_1}$$

$$N_{(1),2}=N_{1,\underline{2}}\times m_{A_2}$$

$$N_{1,2} = N_{1,\underline{2}} \times (\boldsymbol{m}_{A_1} \times DEC_{sp_2 \rightarrow sp_1} + \boldsymbol{m}_{A_2})$$







## Species selection and mixing: Considering the ecological niches and especially the climate envelopes



Waldwachstumskunde Systemanalyse Species mixing: Considering species complementary

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### Potential problems: N. spruce and E. beech Oderhaus/Harz and E. beech s. oak/Steigerwald



Lüpke v. B. and Spellmann, H (1997), Pretzsch and Zenner (2017) Pretzsch (2018)





#### Species mixing: Spatial and temporal separation





Reform workshop in Valladolid/Spain, November 20-21, 2019





Application of guidelines for tree number reduction in mixtures: (1) max. density problem (2) growing space differences







### Problem 1: Max. density modification coefficients, DMC

DMC = max. density mixed/max. density pure stand

Max. density mixed stand = max. density pure stand × DMC

DMC = 1.00 - 1.36





#### Application of DMC, DEC and density reduction







#### Problem 2: Different density, equivalence coefficients DEC

 $N_1 \times DEC_{1\rightarrow 2} = N_2$   $DEC_{1\rightarrow 2} = SDImax_2 / SDImax_1$  DEC = 0.30 - 1.80





#### Application of DMC, DEC and density reduction







# Formulas for mixing regulation with the Density equivalence coefficient

Species proportion of numbers of trees ( $m_{N1}$ ,  $m_{N2}$ , where  $m_{N1}+m_{N2}=1$ )

$$N_{1,(2)} = N_{1,\underline{2}} \times (1/\text{DEC}_{sp_2 \to sp_1} + 1/m_{N_1} - 1)^{-1}$$

$$N_{(1),2} = N_{1,\underline{2}} \times (1/(\text{DEC}_{sp_2 \to sp_1} \times m_{N_2}) - 1/\text{DEC}_{sp_2 \to sp_1} + 1)^{-1}$$

$$N_{1,2} = N_{1,\underline{2}} \times \times \left( (1/\text{DEC}_{sp_2 \to sp_1} + 1/m_{N_1} - 1)^{-1} + (1/(\text{DEC}_{sp_2 \to sp_1} \times m_{N_2}) - 1/\text{DEC}_{sp_2 \to sp_1} + 1)^{-1} \right)$$

Species proportion by area ( $m_{A1}$ ,  $m_{A2}$ , where  $m_{A1}+m_{A2}=1$ )

$$N_{1,(2)} = N_{1,\underline{2}} \times m_{A_1} \times DEC_{sp_2 \rightarrow sp_1}$$

$$N_{(1),2} = N_{1,\underline{2}} \times m_{A_2}$$

$$\mathbf{N}_{1,2} = \mathbf{N}_{1,\underline{2}} \times (\mathbf{m}_{\mathbf{A}_1} \times \mathrm{DEC}_{\mathbf{sp}_2 \to \mathbf{sp}_1} + \mathbf{m}_{\mathbf{A}_2})$$

Pretzsch and del Río (accepted) Density regulation of mixed and monospecific forest stands...Forestry





#### Perspective. Next steps

- Further tests and implementation of DMC, DEC
- Further quantitative formulation of silvicultural guidelines for mixed stands (crop tree selection and release, frequency of th.)
- Algorithmic formulation and integration into models and simulators
- Treatment concepts for long-term experimental plots





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Example of Density Equivalence Coefficients, DEC, for E. beech $\rightarrow$ N. spruce and E. beech $\rightarrow$ S. pine

d <sub>q</sub> d <sub>q</sub> Norway spruce						
E. beech	10	20	25	30	40	50
10	1.27	0.41	0.28	0.21	0.13	0.09
20	4.70	1.50	1.04	0.77	0.48	0.33
25	7.16	2.28	1.58	1.17	0.73	0.50
30	10.10	3.22	2.23	1.65	1.03	0.71
40	17.39	5.54	3.83	2.84	1.76	1.22
50	26.49	8.44	5.84	4.32	2.69	1.86
dq	d <sub>q</sub> Scots pine					
E. beech	10	20	25	30	40	50
10	0.85	0.24	0.16	0.12	0.07	0.05
20	3.13	0.91	0.61	0.44	0.26	0.18
25	4.77	1.38	0.93	0.67	0.40	0.27
30	6.72	1.95	1.31	0.94	0.56	0.38
40	11.57	3.35	2.25	1.62	0.97	0.65
50	17.63	5.10	3.42	2.47	1.48	0.99

